

Credit

Straight Line Theory

$m < 0$ $m = 0$ $m > 0$

Possible values for gradient

Graph of $y = mx + c$

Note: $2y + 4x = 8$
rearrange into correct form
 $y = -2x + 4$

Straight Line
 $y = mx + c$

Two points needed (x_1, y_1) and (x_2, y_2) to calculate gradient

Parallel lines have same gradient

$m = \text{gradient}$ $m = \frac{y_2 - y_1}{x_2 - x_1}$

$C = y$ intercept $(0, C)$

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Functions & Quadratics

Roots $a > 0$

Mini. Point

Line of Symmetry half way between roots

Max. Point

Line of Symmetry half way between roots

$a < 0$

Graphs

Quadratic Functions
 $y = ax^2 + bx + c$

Decimal places

Cannot Factorise

Factorisation
 $ax^2 + bx + c = 0$

SAC
e.g. $(x+1)(x-2) = 0$

Roots
 $x = -1$ and $x = 2$

Roots
 $x = -1.2$ and $x = 0.7$

$f(x) = x^2 + 4x + 3$
 $f(-2) = (-2)^2 + 4(-2) + 3 = -1$

Evaluating

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Mixed Fractions

Adding $\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$

Subtracting $\frac{3}{4} - \frac{1}{2} = \frac{1}{4}$

Simple fractions

Division $\frac{1}{2} \div \frac{3}{5} = \frac{5}{6}$

Flip and change the sign

Basic Rules of Fraction

Harder fractions

Subtracting $2\frac{1}{2} - 1\frac{1}{3} = 1\frac{1}{6}$

Same idea for addition

Multiplication $\frac{1}{2} \times \frac{3}{4} = \frac{3}{8}$

Top-heavy

Division $\frac{1}{2} \div \frac{3}{5} = \frac{5}{6}$

Flip and change the sign

Top-heavy $\frac{3}{2} \times \frac{5}{4} = \frac{15}{8}$

Credit

Simultaneous Equations

Where two lines intersect (crossover)

$y = -2x + 6$

$y = 0.5x + 1$

Graphically

Algebraically

Simultaneous Equations

$2y = x + 2$ $y = -2x + 6$

1. Rearrange & Label

$-x + 2y = 2$ (A)

$2x + y = 6$ (B)

2. Scale and Eliminate

$-2x + 4y = 4$ (C)

$2x + y = 6$ (D)

$5y = 10$

$y = 2$

$-x + 2.2 = 2$

$-x = -2$

$x = 2$

Remember to do the check !!!

$(2, 2)$

Credit

Standard Deviation

x	x^2
2	4
5	25
3	9
5	25
$\Sigma x = 15$	$\Sigma x^2 = 63$
$(\Sigma x)^2 = 225$	

$s_{dev} = \sqrt{\frac{63 - \frac{225}{4}}{3}} = 1.8$

Note
 $mean = \frac{\Sigma x}{n} = \frac{15}{4} = 3.75$

Standard Deviation
"a measure of spread only"

$S = \text{standard deviation}$
 $n = \text{number of data points}$
 $(\Sigma x)^2 = \text{Sum of data squared}$
 $\Sigma x^2 = \text{Sum of squared data}$

$s_{dev} = \sqrt{\frac{\Sigma x^2 - \frac{(\Sigma x)^2}{n}}{n-1}}$

Credit

Area and Volume (Prisms)

Rectangle: $A = L \times B$

Circle: $A = \pi r^2$

Triangle: $A = \frac{1}{2}bh$

Rectangular Prism: $V = L \times B \times H$

Cylinder: $V = \pi r^2 h$

Simple Areas

Simple Volume

Area & Volume of a Prism

Volume = Area x Height

Composite Areas

Composite Volume

made up of basic areas

made up of basic volumes

$A = L \times B + \frac{1}{2}bh$

$V = (L \times B \times H) + (\frac{1}{2}BhL)$

Credit

Circle Properties

Arc length is a fraction of the circumference

$\frac{Arc_{length}}{\pi D} = \frac{Angle}{360}$

Pythagoras Theorem SOHCAHTOA

A line that bisects a chord

- Splits the chord into 2 equal halves
- Makes right-angle with the chord
- Passes through centre of the circle

Semi-circle angle is always 90°

Circumference is $C = \pi D$

Tangent touches circle at one point and make angle 90° with point of contact radius

Diameter $D = 2r$

Radius $r = \frac{1}{2}D$

Area is $A = \pi r^2$

Sector area is a fraction of the whole area

$\frac{AoS}{\pi r^2} = \frac{Angle}{360}$

Credit

Harder Percentages

80% \Rightarrow £500

100% is original price

$\frac{100}{80} \times 500 = \text{£625}$

Higher OR Lower price?

Original price

A TV is reduced by 20% to £500. What was the original price?

Percentage year on year

Percentage out of 100

How much will I have in the bank if I invest £80 over 10 years at 5% interest?

$V = 80 \left(1 + \frac{5}{100}\right)^{10}$

$V = \text{£130.31}$

$V = I \left(1 + \frac{\%}{100}\right)^n$

$V = \text{value}$ $I = \text{initial}$ $n = \text{time}$

Credit

Factorisation

$2x^2 - 7x + 6$

Possibly mixed Common factor then SAC

St. Andrew's Cross Method (3 terms)

Factorisation "product of brackets"

Common factor

Difference of 2 squares

Mixed

e.g. $4y - 8y^2$
 $4y(1-2y)$

$4x^2 - 36$
 $4(x^2 - 9)$
 $4(x+3)(x-3)$

e.g. $9m^2 - 64$
 $(3m+8)(3m-8)$