

## $M\alpha$ the matics

## National 5 Practice Paper A

Paper 2

Duration - 1 hour and 30 minutes

Total marks - 50

- You may use a calculator
- Attempt all the questions.
- Use blue or black ink.
- Full credit will only be given to solutions which contain appropriate working.
- State the units for your answer where appropriate.

1. The population of a city is increasing at a steady rate of 2.4% per annum. The current population is 528 000.

What is the expected population in 4 years?

Give your answer to the nearest thousand.

- 2. Two groups of 6 students are given the same test.
  - (a) The marks of Group A are:

73 47 59 71 48 62.

Use an appropriate formula to calculate the mean and the standard deviation.

Show clearly all your working.

(b) In Group B, the mean is 60 and the standard deviation is 29.8.

Compare the results of the two groups.

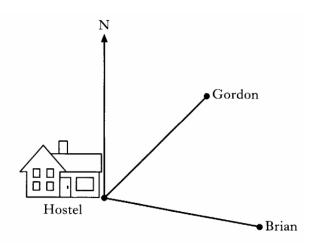
3. Multiply out the brackets and collect like terms.

$$(x+4)(2x^2+3x-1)$$
 3

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Gordon and Brian leave a hostel at the same time.
Gordon walks on a bearing of 045° at a speed of 4.4 kilometres per hour.
Brian walks on a bearing of 100° at a speed of 4.8 kilometres per hour.



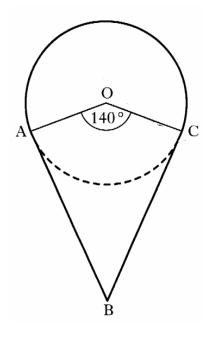
If they both walk at stead speeds, how far apart will they be after 2 hours?

5. The diagram shows a mirror which has been designed for a new hotel.

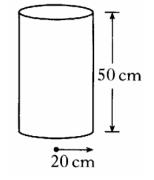
The shape consists of a sector of a circle and a kite AOCB.

- The circle, centre O, has a radius of 50 centimetres.
- $\circ$  Angle AOC = 140°
- AB and CB are tangents to the circle at A and C respectively.

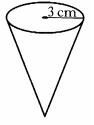
Find the perimeter of the mirror.



- A drinks container is in the shape of a 6. cylinder with radius 20 centimetres and height 50 centimetres.
  - Calculate the volume of the drinks (a) container. Give your answer in cubic centimetres, correct to two significant figures.

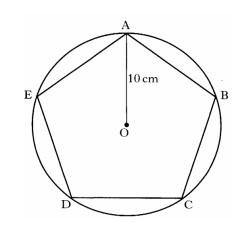


Liquid from the full container can fill 800 cups, in the shape of cones, (b) each of radius 3 centimetres.



What will be the height of liquid in each cup?

7.



A regular pentagon ABCDE is drawn in a circle, centre 0, with radius 10 centimetres. Calculate the area of the regular pentagon.

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8. (a) Express  $a^2 \left(2a^{-\frac{1}{2}} + a\right)$  in its simplest form.

## (b) Use an appropriate formula to solve the quadratic equation

$$3x^2 + 3x - 7 = 0.$$

Give your answers correct to 1 decimal place.

$$4 \tan x^{\circ} + 5 = 0, \quad 0 \le x \le 360.$$
 3

(b) Show that

$$\tan x \cos x = \sin x.$$

National 5 Practice Paper A

2

| - | - | - | - | - |   |
|---|---|---|---|---|---|
| - |   | 4 |   | - |   |
| - |   | - |   |   | _ |
| 6 |   | 6 |   | - |   |
| - |   | 4 |   | - |   |
| - |   | - |   | - |   |
| 6 | - | 1 |   | - | - |
| E | 1 | 1 |   | 2 | 1 |

It is to be enlarged by increasing both the length and the width by x centimetres.

(a) Show that the area, A square centimetres, of the new vent is given by  $A = x^2 + 40x + 300.$ 

The area of the new vent must be at least 75% more than the original area.

(b) Find the minimum dimensions of the new vent.